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# Investigating the effects of fuel injection strategies on a dual-fuel diesel-H<sub>2</sub> compression ignition engine

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Article info:		Abstract
Type: Received: Revised: Accepted: Online:	Research 06/06/2019 01/10/2019 05/10/2019 05/10/2019	In this computational research, separate and simultaneous impacts of diesel direct injection timing, fuel spraying cone angle, and hydrogen gas addition on combustion characteristics, output emissions, and performance in a single-cylinder direct injection diesel engine were studied. In order to conduct the simulations, valid and reliable models for combustion, break-up, and turbulence
Online:05/10/2019Keywords:Combustion,Simulation,Dual-fuel,Injection timing,Fuel spray angle,Emission.		Were used. The effects of fifteen fuel injection strategies based on characteristics such as time of fuel spraying (-15, -10 CA BTDC, and TDC) and nozzle cone angle (105, 115, 125, 145, and 160 degrees) under neat diesel combustion and diesel-hydrogen combustion engine operations conditions were explored. The obtained results indicated that the addition of H <sub>2</sub> due to significant heating value increases indicated power and improves indicated specific energy consumption at the expense of NO <sub>x</sub> emissions, but considerably decreases CO and soot emissions simultaneously. By advancing injection timing, maximum pressure peak point, maximum temperature peak point, and maximum heat release rate peak point increase and cause lower indicated specific energy consumption. However, using a wide spray angle (e.g., 160 cone degrees) results in lower indicated power and higher indicated specific energy consumption due to the fact that more fuel could spray in regions with lower oxygen concentrations as compared to baseline operation case.

### 1. Introduction

Due to lower energy consumption, higher thermal efficiency, and less CO and  $CO_2$ emissions compared to spark ignition and gas engines, compression ignition known as diesel engines are widely used in transportation, agriculture, and also powering stationary/mobile equipment [1-2]. However, because of the type of combustion, they produce a high level of  $NO_x$ and PM emissions. To reduce pollutant emissions and meet stringent emission regulations, extensive studies and investigations have been conducted by many researchers [3-10]. Kim et al. [11] have investigated the effects of nozzle cone angle and time of fuel spraying on the combustion and emissions in a HSDI compression ignition engine. The engine they have used for their study is a single-cylinder equipped with Bosch common rail direct injection system. Their results showed that, spraying fuel by 60 degrees cone angle was accompanied by higher MPPP, MHRRPPP, and shorter ignition delay period compared to 156 degrees. In the case of emissions formation, they indicated that using narrow spray angle simultaneous with early injection timing resulted in low UHC, CO, and  $NO_x$  emissions. Also, IMEP for a narrow nozzle cone angle is higher than 156 degrees cone angle.

Benajes et al. [12] have explored the influences of blending ratio and fuel spray timing. Their case study was RCCI combustion in a singlecylinder diesel engine. Their results showed that retarding the combustion phasing near TDC point has promoted an increase in  $NO_x$ emissions. Furthermore, advancing diesel direct injection timing has led to diminishing soot at low load. They also reported that by retarding the injection timing amounts of CO, UHC, and soot emissions have considerably increased.

The clean combustion of hydrogen which produces zero CO2, CO, UHC, and PM emissions attracted lots of attention to use H2 gas as a clean fuel for internal combustion engines, especially diesel engines. For years, lots of studies have been done in order to explore the possibility and impacts of using H<sub>2</sub> gas on the combustion process, emissions formation, and performance in diesel engines [13-15]. In their paper, Christodoulou and Megaritis [16] have examined the effects of hydrogen gas addition on the pollutant emissions and combustion of a DI diesel engine. The engine they used for their study was a four-cylinder, HSDI compression ignition. Their results showed that hydrogen gas addition had decreased PM and CO, but NO<sub>x</sub> emissions have considerably increased. Also, increasing hydrogen concentration has reduced CO emissions since mixtures of carbon/ hydrogen ratio has decreased.

This numerical research aims to explore the influences of using  $H_2$  addition and diesel direct injection strategies in a heavy-duty diesel engine. This study is divided into three sections; the first part discusses the effects of hydrogen gas addition and fuel direct injection characteristics such as fuel spray timing and nozzle cone angle on in-cylinder pressure, temperature, and heat release rate. In the second and third parts, the effects of studying strategies on emissions formation (such as NOx, soot, and

CO) and engine performance will be discussed respectively.

### 2. Model description

AVL ESE Fire code and its tools were used to numerically predict Diesel-H<sub>2</sub> dual-fuel combustion and also, creating computational grid [17]. Due to the symmetrical shape of combustion chamber and using a six-holes nozzle, computations conducted on 60 degrees segement. Table 1 shows some of the computational grid specifications. Fig. 1 shows the computational grid at TDC.

Extended Coherent Flame Model 3 Zone (ECFM-3Z) was used for simulating premixed and diffusice combustion [17]. In order to take auto-ignition and flame propagation into account, this model temporarily combines fuel components to a fuel mixture during calculations [18-19]. Also, transport equations of ECFM-3Z were able to solve the averaged quantities of species such as N, N<sub>2</sub>, O, O<sub>2</sub>, CO, CO<sub>2</sub>, H, H<sub>2</sub>, OH, H<sub>2</sub>O, and NO [17].

K-Zeta-F model was applied for simulating the turbulence flow inside the combustion chamber. This model was developed in 2004 by Hanjalic, Popovac, and Hadziabdic [20]. In order to enhnce the stability of the  $v^2$ -f model, the authors introduced a form of an eddy viscosity based on Durbin's elliptic relaxation concept [17].

Table 1. Computational grid specifications.			
Number of boundary layers (-)	2		
Thickness of boundary layer (mm)	0.2		
Average cell area size (mm)	1.2		
Number of cells at IVC event (-)	77650		
Number of cells at TDC (-)	31300		



Fig. 1. The computational grid at TDC.

Also, they provided a merging formula for the quantities determined at the cells near the wall as:

$$\varphi_p = \varphi_v e^{-\Gamma} + \varphi_t e^{-1/\Gamma} \tag{1}$$

Where v is viscous, t is the fully turbulent value of the wall shear stress, production, and dissipation of the turbulent kinetic energy respectively [17].

Dukowicz model [21] was used to predict the fuel parcels evaporation process. In order to model the first and second breakup of fuel sprayed particles, Kelvin-Helmholtz coupled with Rayleigh-Taylor mechanism was used [22]. The Kelvin-Helmholtz mechanism is responsible for high velocities. Furthermore, the Rayleigh-Taylor mechanism is able to predict the time and length of the second breakup of the injected fuel parcels [17]. Also, Nordin collision model was used for taking the fuel particles interactions into account [23]. Along with other sub-models, Naber and Reitz method [24] was applied for simulating the fuel particles and wall interactions.

Finally, Extended Zeldovich + Prompt + Fuel and Hiroyasu/Nagle/Strickland-Constable models were used for calculating the exhaust gas NO<sub>x</sub> and soot emissions formation, respectively [17].

# **3.** Engine specifications, experimental Setup, and model validation

A heavy-duty single-cylinder turbocharged DI diesel engine known as caterpillar 3401, was used for this numerical research [25]. The engine and fuel injection system specifications are presented in Table 2 and Table 3, respectively [25]. Table 4 and Table 5 show the Diesel and H<sub>2</sub> fuels specifications respectively.

The experimental in-cylinder pressure and HRR trends were averaged from 499 working cycles [25]. The results obtained from the calculations are based on the assumption of a uniform wall temperature of 520 K for the cylinder head and the piston top and 420 K for the cylinder wall.

Fig. 2 reports the comparison of measured and calculated in-cylinder pressure and HRR results [25].

Table 2. Engine specifications

Engine type	Heavy-duty turbo- charged diesel engine				
Bore (mm) x stroke (mm)	137.16 x 165.1				
Geometric compression ratio	16.1:1				
Displacement volume (L)	2.44				
Connecting rod length (mm)	261.6				
TDC clearance gap (mm)	1.97				
Engine speed (rpm)	1208				
Bowl volume (cc)	110.8				
IVC (CA BTDC)	143				
EVO (CA BTDC)	-130				
IMAP (bar)	2.0				
IMAT (K)	313				

Table 3.	Fuel in	njection	system	specifications.
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Injector holder	Bosch CRIN 2
Number of injector holes	6
Spray angle (degree)	145
Nozzle hole diameter (mm)	0.25
Injection pressure (bar)	755
Total fuel per cycle (mg)	172.2
Fuel injection timing (CA BTDC)	10
Fuel injection duration (CA)	16.8

 Table 4. Diesel fuel specifications [25].

Specific gravity @ 15.5 C (-)	0.856
Viscosity @ 40 C (cSt)	2.71
Lower heating value (MJ/Kg)	42.526
Cetane number	46.1

Table 5. Hydrogen gas specifications [28].					
Property	Unit	Values			
Adiabatic flame temperature ( $\varphi = 1$ )	[K]	2480			
Auto ignition temperature in air	[K]	858			
Density	$[kg/m^3]$	0.0824			
Flame velocity ( $\varphi = 1$ )	$[ms^{-1}]$	1.85			
Lower heating value	[MJ/kg]	119.7			



**Fig. 2.** Comparison of measured and calculated results of in-cylinder mean pressure and rate of heat release under baseline condition [25].

As indicated in Fig. 2, the in-cylinder mean pressure and HRR modeled by the Fire code are reasonably close to measured results. However, there are some discrepancies as reported in Fig. 2 that could be linked to experimental uncertainties such as IMAT, duration of injection, and or exact SOI [26, 27]. Table 6 shows the comparison of measured and calculated engine output emissions under the baseline operation condition. As reported in Table 6, emissions formation are well simulated by the CFD Fire code compared with experimental results.

#### 4. Modeling methodology

This study aims to examine the impacts of fuel injection strategies on the combustion process of heavy-duty dual-fuel compression ignition engine. Direct diesel injection timing and nozzle cone angle are the two variables that their effects are the primary purpose of this numerical study. In addition to baseline operation case, 15 fuel spraying strategies based on the fuel DI characteristics such as spray timing (-15, -10 CA BTDC, and TDC) and nozzle cone angle (105, 115, 125, 145, and 160 degrees) have been considered and their influences on the combustion specifications (in-cylinder mean temperature, pressure, and HRR), emissions formation (NO<sub>x</sub>, soot, and CO), and engine performance (ISEC and IP) under NDC and (80-20%) energy fraction) engine DHC operations conditions were investigated. Finally, the obtained results of this computational research have been presented in detail in the form of charts and figures.

#### 5. Results and discussion

5.1. Influence of study strategies on the combustion specifications

Fig. 3 shows the effects of hydrogen addition on in-cylinder pressure, temperature, and HRR. As can be seen in Fig. 3, using of  $H_2$  gas led to increasing the in-cylinder MPPP, MTPP, and MHRRPP. High heating value and fast combustion rate of  $H_2$  gas led to improving the air-fuel mixture oxidation process for DHC case compared to NDC mode.

Table (	5. C	omparise	on of nume	erical and ex	xperime	ntal
results	of	output	pollutant	emissions	under	the
baseline	e op	eration of	condition [2	25].		

Emissions (g/kg. fuel)	NOx	CO	Soot
Current research	52.91	2.75	0.27
Experimental	49.8	3.1	0.31



**Fig. 3.** Impacts of hydrogen addition on combustion specifications.

Fig. 4 shows the influences of spray timing on in-cylinder mean pressure, temperature, and HRR. As illustrated in Fig. 4, advancing direct injection timing has increased MPPP, MTPP, and MHRRPP. While retarding the injection timing has opposite effects.

In direct injection compression ignition engines, the heat release process consists of premixed and diffusive combustion [29]. Initially, combustion occurs in the premixed burning mode until the air-fuel mixure which formed during the ignition delay period is ready for ignition; then, the rest of the evaporated air-fuel mixture will burn in diffusive combustion mode and this continues until the end of the heat release period. By advancing direct spray timing, due to lower incylinder pressure and temperature compared to baseline operation case, ID period has been extended.

More extended ID period leads to more fuel to be evaporated and accumulated and burn in premixed combustion mode. Due to the high rate premixed combustion, pressure of and temperature rise rate for advanced ITs could be increased and as illustrated in Fig. 4, for 15 CA BTDC IT, the MPPP, MTPP, and MHRRPP compared to baseline case have increased. However, by retarding the fuel spray timing due to higher in-cylinder pressure and temperature compared to the baseline case, ID period could be shortened, and most of the evaporated fuel burns in diffusive combustion mode. In addition to that, diffusive combustion leads to lower pressure and temperature rise rate and as can be seen in Fig. 4, TDC IT has decreased MPPP, MTPP, and MHRRPP compared to baseline operation case.



**Fig. 4.** Impacts of fuel spray timing on combustion specifications.

Fig. 5 shows the influences of fuel spraying angle on in-cylinder mean pressure, temperature, and HRR. As illustrated in Fig. 5, by increasing fuel spray angle MPPP, MTPP, and MHRRPP have increased.

Proper fuel spray angle causes the fuel to be sprayed in regions with higher oxygen concentrations that lead to improvement of the mixture oxidation process, and as can be seen in Fig. 5, MPPP, MTPP, and MHRRPP have increased.

# 5.2. Effects of study strategies on the emissions formation

Fig. 6 shows the impacts of fuel spray timing, fuel spraying angle, and  $H_2$  gas addition on NOx and soot emission. As illustrated in Fig. 6, the use of hydrogen gas has considerably decreased soot emission for all injection timings and fuel spraying angles at the expense of NOx emissions.



Fig. 5. Effects of study strategies on combustion characteristics.

Induction of  $H_2$  gas and participating in the combustion process due to higher heating value compared to diesel fuel led to higher MPPP, MTPP, and MHRRPP. As a result, air-fuel mixture oxidation has improved and led to higher NOx and lower soot emissions compared to NDC mode. As illustrated in Fig. 6, by advancing the direct injection timing, the amount of NO<sub>x</sub> emissions have increased.

Advanced ITs led to more evaporated fuel burns in premixed combustion that could increase pressure and temperature rise rate of compression ignition combustion, and as reported in Fig. 6, the amounts of NO<sub>x</sub> emissions increased. Furthermore, increasing the fuel spraying angle due to a better air-fuel mixture formation led to decrease in the soot emission considerably. It must be mentioned that for TDC IT, injecting fuel with 160 degrees as spraying cone angle led to increasing soot emission that must be due to more fuel sprayed in a region with low oxygen concentration.



**Fig. 6.** Effects of study strategies on the soot-NOx trade-off.

Fig. 7 shows the influences of fuel spray timing, fuel spraying angle, and  $H_2$  gas addition on  $NO_x$ and CO emission. As indicated in Fig. 7, by the addition  $H_2$  into the combustion chamber, the amount of CO emission has decreased considerably. In other words, by replacing a part of the diesel fuel with  $H_2$  gas, the amount of fuel carbon species that participates in combustion has decreased, and as a result, CO emission has diminished as compared to NDC mode.

Furthermore, retarding the injection timing due to lower MPPP, MTPP, and MHRRPP caused by more evaporated fuel, which burned in diffusive combustion mode, led to higher CO emission. As presented in Fig. 7, a wider spray cone angle led to lower CO emission due to better air-fuel mixing that has improved fuel oxidation process.

# 5.3. Effects of study strategies on engine performance

Fig. 8 reports the effects of fuel spray timing, fuel spraying angle, and  $H_2$  gas addition on IP and ISEC.



Fig. 7. Impacts of study strategies on the CO-NOx trade-off.

As illustrated in Fig. 8, the use of  $H_2$  has improved increased IP and **ISEC** simultaneously. In other words, the addition of hydrogen gas due to high heating value led to increasing the MPPP, MTPP, and MHRRPP that resulted in the improved fuel oxidation process. Better air-fuel mixture oxidation could improve engine performance, especially lower ISEC compared to NDC mode. Advancing the direct injection timing has increased the IP and decreased ISEC simultaneously. For advanced ITs, more evaporated fuel could burn in premixed combustion that led to higher pressure and temperature rise rate. As a result, MPPP, MTPP, and MHRRPP increased, and engine performance improved. Furthermore, increasing the fuel spray cone angle due to better air-fuel mixing and improved fuel oxidation increased the IP and improved the ISEC. However, 160 angle decreased degrees cone engine performance due to the fact that more fuel could be sprayed in regions with lower oxygen level that led to lean mixture formation and oxidation.

#### 6. Conclusions

In the present study, the separate and simultaneous effects of diesel fuel spray timing, nozzle cone angle, and addition of  $H_2$  gas on combustion characteristics, output pollutant emissions, and performance of a single-cylinder heavy-duty compression ignition engine were examined. The obtained results revealed that:

- Induction of  $H_2$  gas into the engine cylinder has increased MPPP, MTPP, and MHRRPP compared to NDC mode. Also, higher combustion temperature has improved mixture oxidation, and as a result, soot and CO emissions significantly have decreased. However, because of the high heating value of  $H_2$  gas and higher combustion temperature of  $H_2$ -Diesel compared to NDC mode, NO<sub>x</sub> emissions have increased.

- Advancing fuel DI timing led to a longer ID period. More extended ID accompanied by more evaporated fuel to ignite in premixed combustion, which resulted in higher pressure and temperature rise rate that could increase MPPP, MTPP, and MHRRPP. As a result, the air-fuel mixture formation has improved, and following that, soot and CO emissions have diminished.



**Fig. 8.** Effects of study strategies on the IP-NOx and the ISEC-NO<sub>x</sub> trade-off.

- Simultaneous addition of H2 gas and advancing the fuel DI timing led to the improvement of ISEC and increasing IP at the expanse of high NO<sub>x</sub> emissions.

- Wide fuel spray cone angle (e.g., 160 degrees) led to more fuel to spray in regions with lower oxygen concentrations that could decrease IP and increase ISEC simultaneously.

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